

TEST PAPER OF JEE(MAIN) EXAMINATION – 2019
(Held On SATURDAY 12th JANUARY., 2019) TIME : 09 : 30 AM To 12 : 30 PM
MATHEMATICS

1. For $x > 1$, if $(2x)^{2y} = 4e^{2x-2y}$, then

$(1 + \log_e 2x)^2 \frac{dy}{dx}$ is equal to :

- (1) $\log_e 2x$
(2) $\frac{x \log_e 2x + \log_e 2}{x}$
(3) $x \log_e 2x$
(4) $\frac{x \log_e 2x - \log_e 2}{x}$

Ans. (4)

2. The sum of the distinct real values of μ , for which the vectors, $\mu \hat{i} + \hat{j} + \hat{k}$, $\hat{i} + \mu \hat{j} + \hat{k}$, $\hat{i} + \hat{j} + \mu \hat{k}$ are co-planer, is :

- (1) 2 (2) 0 (3) -1 (4) 1

Ans. (3)

3. Let S be the set of all points in $(-\pi, \pi)$ at which the function, $f(x) = \min \{ \sin x, \cos x \}$ is not differentiable. Then S is a subset of which of the following?

- (1) $\left\{ -\frac{3\pi}{4}, -\frac{\pi}{4}, \frac{3\pi}{4}, \frac{\pi}{4} \right\}$
(2) $\left\{ -\frac{3\pi}{4}, -\frac{\pi}{2}, \frac{\pi}{2}, \frac{3\pi}{4} \right\}$
(3) $\left\{ -\frac{\pi}{2}, -\frac{\pi}{4}, \frac{\pi}{4}, \frac{\pi}{2} \right\}$
(4) $\left\{ -\frac{\pi}{4}, 0, \frac{\pi}{4} \right\}$

Ans. (1)

4. The product of three consecutive terms of a G.P. is 512. If 4 is added to each of the first and the second of these terms, the three terms now form an A.P. Then the sum of the original three terms of the given G.P. is

- (1) 36 (2) 24
(3) 32 (4) 28

Ans. (4)

5. The integral $\int \cos(\log_e x) dx$ is equal to :

(where C is a constant of integration)

- (1) $\frac{x}{2} [\sin(\log_e x) - \cos(\log_e x)] + C$
(2) $\frac{x}{2} [\cos(\log_e x) + \sin(\log_e x)] + C$
(3) $x [\cos(\log_e x) + \sin(\log_e x)] + C$
(4) $x [\cos(\log_e x) - \sin(\log_e x)] + C$

Ans. (2)

6. Let $S_k = \frac{1+2+3+\dots+k}{k}$. If

$S_1^2 + S_2^2 + \dots + S_{10}^2 = \frac{5}{12} A$, then A is equal to :

- (1) 303 (2) 283 (3) 156 (4) 301

Ans. (1)

7. Let $S = \{1, 2, 3, \dots, 100\}$. The number of non-empty subsets A of S such that the product of elements in A is even is :-

- (1) $2^{50}(2^{50}-1)$ (2) $2^{100}-1$
(3) $2^{50}-1$ (4) $2^{50}+1$

Ans. (1)

8. If the sum of the deviations of 50 observations from 30 is 50, then the mean of these observations is :

- (1) 50 (2) 51 (3) 30 (4) 31

Ans. (4)

9. If a variable line, $3x+4y-\lambda=0$ is such that the two circles $x^2 + y^2 - 2x - 2y + 1 = 0$ and $x^2+y^2-18x-2y+78 = 0$ are on its opposite sides, then the set of all values of λ is the interval :-

- (1) [12, 21] (2) (2, 17)
(3) (23, 31) (4) [13, 23]

Ans. (1)

10. A ratio of the 5th term from the beginning to the 5th term from the end in the binomial

expansion of $\left(2^{\frac{1}{3}} + \frac{1}{2(3)^{\frac{1}{3}}}\right)^{10}$ is :

- (1) $1 : 4(16)^{\frac{1}{3}}$ (2) $1 : 2(6)^{\frac{1}{3}}$
 (3) $2(36)^{\frac{1}{3}} : 1$ (4) $4(36)^{\frac{1}{3}} : 1$

Ans. (4)

11. let C_1 and C_2 be the centres of the circles $x^2+y^2-2x-2y-2 = 0$ and $x^2+y^2-6x-6y+14 = 0$ respectively. If P and Q are the points of intersection of these circles, then the area (in sq. units) of the quadrilateral PC_1QC_2 is :

- (1) 8 (2) 6 (3) 9 (4) 4

Ans. (4)

12. In a random experiment, a fair die is rolled until two fours are obtained in succession. The probability that the experiment will end in the fifth throw of the die is equal to :

- (1) $\frac{150}{6^5}$ (2) $\frac{175}{6^5}$ (3) $\frac{200}{6^5}$ (4) $\frac{225}{6^5}$

Ans. (2)

13. If the straight line, $2x-3y+17 = 0$ is perpendicular to the line passing through the points (7, 17) and (15, β), then β equals :-

- (1) -5 (2) $-\frac{35}{3}$ (3) $\frac{35}{3}$ (4) 5

Ans. (4)

14. Let f and g be continuous functions on $[0, a]$ such that $f(x) = f(a-x)$ and $g(x)+g(a-x)=4$,

then $\int_0^a f(x)g(x)dx$ is equal to :-

- (1) $4\int_0^a f(x)dx$ (2) $2\int_0^a f(x)dx$
 (3) $-3\int_0^a f(x)dx$ (4) $\int_0^a f(x)dx$

Ans. (2)

15. The maximum area (in sq. units) of a rectangle having its base on the x-axis and its other two vertices on the parabola, $y = 12-x^2$ such that the rectangle lies inside the parabola, is :-

- (1) $20\sqrt{2}$ (2) $18\sqrt{3}$ (3) 32 (4) 36

Ans. (3)

16. The Boolean expression

$((p \wedge q) \vee (p \vee \sim q)) \wedge (\sim p \wedge \sim q)$ is equivalent to:

- (1) $p \wedge (\sim q)$ (2) $p \vee (\sim q)$
 (3) $(\sim p) \wedge (\sim q)$ (4) $p \wedge q$

Ans. (3)

17. $\lim_{x \rightarrow \pi/4} \frac{\cot^3 x - \tan x}{\cos(x + \pi/4)}$ is :

- (1) 4 (2) $8\sqrt{2}$ (3) 8 (4) $4\sqrt{2}$

Ans. (3)

18. Considering only the principal values of inverse functions, the set

$$A = \{x \geq 0 : \tan^{-1}(2x) \tan^{-1}(3x) = \frac{\pi}{4}\}$$

- (1) is an empty set
 (2) Contains more than two elements
 (3) Contains two elements
 (4) is a singleton

Ans. (4)

19. An ordered pair (α, β) for which the system of linear equations

$$(1+\alpha)x + \beta y + z = 2$$

$$\alpha x + (1+\beta)y + z = 3$$

$\alpha x + \beta y + 2z = 2$ has a unique solution is

- (1) (1, -3) (2) (-3, 1)
 (3) (2, 4) (4) (-4, 2)

Ans. (3)

20. The area (in sq. units) of the region bounded by the parabola, $y = x^2 + 2$ and the lines, $y = x + 1$, $x = 0$ and $x = 3$, is :

- (1) $\frac{15}{4}$ (2) $\frac{15}{2}$ (3) $\frac{21}{2}$ (4) $\frac{17}{4}$

Ans. (2)

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21. If λ be the ratio of the roots of the quadratic equation in x , $3m^2x^2+m(m-4)x+2=0$, then the

least value of m for which $\lambda + \frac{1}{\lambda} = 1$, is :

- (1) $2 - \sqrt{3}$ (2) $4 - 3\sqrt{2}$
(3) $-2 + \sqrt{2}$ (4) $4 - 2\sqrt{3}$

Ans. (2)

22. If the vertices of a hyperbola be at $(-2, 0)$ and $(2, 0)$ and one of its foci be at $(-3, 0)$, then which one of the following points does not lie on this hyperbola?

- (1) $(4, \sqrt{15})$ (2) $(-6, 2\sqrt{10})$
(3) $(6, 5\sqrt{2})$ (4) $(2\sqrt{6}, 5)$

Ans. (3)

23. If $\frac{z-\alpha}{z+\alpha}$ ($\alpha \in \mathbb{R}$) is a purely imaginary number and $|z| = 2$, then a value of α is :

- (1) 1 (2) 2 (3) $\sqrt{2}$ (4) $\frac{1}{2}$

Ans. (2)

24. Let $P(4, -4)$ and $Q(9, 6)$ be two points on the parabola, $y^2 = 4x$ and let X be any point on the arc POQ of this parabola, where O is the vertex of this parabola, such that the area of ΔPXQ is maximum. Then this maximum area (in sq. units) is :

- (1) $\frac{125}{4}$ (2) $\frac{125}{2}$ (3) $\frac{625}{4}$ (4) $\frac{75}{2}$

Ans. (1)

25. the perpendicular distance from the origin to the plane containing the two lines, $\frac{x+2}{3} = \frac{y-2}{5} = \frac{z+5}{7}$ and $\frac{x-1}{1} = \frac{y-4}{4} = \frac{z-4}{7}$, is:

- (1) $\frac{11}{\sqrt{6}}$ (2) $6\sqrt{11}$ (3) 11 (4) $11\sqrt{6}$

Ans. (1)

26. The maximum value of $3\cos\theta + 5\sin\left(\theta - \frac{\pi}{6}\right)$ for any real value of θ is :

- (1) $\sqrt{19}$ (2) $\frac{\sqrt{79}}{2}$ (3) $\sqrt{31}$ (4) $\sqrt{34}$

Ans. (1)

27. A tetrahedron has vertices $P(1, 2, 1)$, $Q(2, 1, 3)$, $R(-1, 1, 2)$ and $O(0, 0, 0)$. The angle between the faces OPQ and PQR is :

- (1) $\cos^{-1}\left(\frac{9}{35}\right)$ (2) $\cos^{-1}\left(\frac{19}{35}\right)$
(3) $\cos^{-1}\left(\frac{17}{31}\right)$ (4) $\cos^{-1}\left(\frac{7}{31}\right)$

Ans. (1)

28. Let $y = y(x)$ be the solution of the differential equation, $x \frac{dy}{dx} + y = x \log_e x$, ($x > 1$). If $2y(2) = \log_e 4 - 1$, then $y(e)$ is equal to :-

- (1) $\frac{e^2}{4}$ (2) $\frac{e}{4}$ (3) $-\frac{e}{2}$ (4) $-\frac{e^2}{2}$

Ans. (2)

29. Let $P = \begin{bmatrix} 1 & 0 & 0 \\ 3 & 1 & 0 \\ 9 & 3 & 1 \end{bmatrix}$ and $Q = [q_{ij}]$ be two 3×3

matrices such that $Q - P^5 = I_3$. Then $\frac{q_{21} + q_{31}}{q_{32}}$ is equal to:

- (1) 15 (2) 9 (3) 135 (4) 10

Ans. (4)

30. Consider three boxes, each containing 10 balls labelled 1, 2, ..., 10. Suppose one ball is randomly drawn from each of the boxes. Denote by n_i , the label of the ball drawn from the i th box, ($i = 1, 2, 3$). Then, the number of ways in which the balls can be chosen such that $n_1 < n_2 < n_3$ is :

- (1) 82 (2) 240 (3) 164 (4) 120

Ans. (4)

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