

**TEST PAPER OF JEE(MAIN) EXAMINATION – 2019**  
**(Held On Friday 11<sup>th</sup> JANUARY, 2019) TIME : 2 : 30 PM To 5 : 30 PM**  
**MATHEMATICS**

1. If the point  $(2, \alpha, \beta)$  lies on the plane which passes through the points  $(3, 4, 2)$  and  $(7, 0, 6)$  and is perpendicular to the plane  $2x - 5y = 15$ , then  $2\alpha - 3\beta$  is equal to :-  
 (1) 5      (2) 17      (3) 12      (4) 7

**Ans. (4)**

2. Let  $\alpha$  and  $\beta$  be the roots of the quadratic equation  $x^2 \sin \theta - x (\sin \theta \cos \theta + 1) + \cos \theta = 0$

$(0 < \theta < 45^\circ)$ , and  $\alpha < \beta$ . Then  $\sum_{n=0}^{\infty} \left( \alpha^n + \frac{(-1)^n}{\beta^n} \right)$

is equal to :-

- (1)  $\frac{1}{1 - \cos \theta} + \frac{1}{1 + \sin \theta}$   
 (2)  $\frac{1}{1 + \cos \theta} + \frac{1}{1 - \sin \theta}$   
 (3)  $\frac{1}{1 - \cos \theta} - \frac{1}{1 + \sin \theta}$   
 (4)  $\frac{1}{1 + \cos \theta} - \frac{1}{1 - \sin \theta}$

**Ans. (1)**

3. Let  $K$  be the set of all real values of  $x$  where the function  $f(x) = \sin |x| - |x| + 2(x - \pi) \cos |x|$  is not differentiable. Then the set  $K$  is equal to :-  
 (1)  $\{\pi\}$       (2)  $\{0\}$   
 (3)  $\phi$  (an empty set)      (4)  $\{0, \pi\}$

**Ans. (3)**

4. Let the length of the latus rectum of an ellipse with its major axis along  $x$ -axis and centre at the origin, be 8. If the distance between the foci of this ellipse is equal to the length of its minor axis, then which one of the following points lies on it ?  
 (1)  $(4\sqrt{3}, 2\sqrt{3})$       (2)  $(4\sqrt{3}, 2\sqrt{2})$   
 (3)  $(4\sqrt{2}, 2\sqrt{2})$       (4)  $(4\sqrt{2}, 2\sqrt{3})$

**Ans. (2)**

5. If the area of the triangle whose one vertex is at the vertex of the parabola,  $y^2 + 4(x - a^2) = 0$  and the other two vertices are the points of intersection of the parabola and  $y$ -axis, is 250 sq. units, then a value of 'a' is :-  
 (1)  $5\sqrt{5}$       (2)  $(10)^{2/3}$       (3)  $5(2^{1/3})$       (4) 5

**Ans. (4)**

6. The integral  $\int_{\pi/6}^{\pi/4} \frac{dx}{\sin 2x (\tan^5 x + \cot^5 x)}$  equals :-

- (1)  $\frac{1}{10} \left( \frac{\pi}{4} - \tan^{-1} \left( \frac{1}{9\sqrt{3}} \right) \right)$   
 (2)  $\frac{1}{5} \left( \frac{\pi}{4} - \tan^{-1} \left( \frac{1}{3\sqrt{3}} \right) \right)$   
 (3)  $\frac{\pi}{10}$   
 (4)  $\frac{1}{20} \tan^{-1} \left( \frac{1}{9\sqrt{3}} \right)$

**Ans. (1)**

7. Let  $(x + 10)^{50} + (x - 10)^{50} = a_0 + a_1x + a_2x^2 + \dots + a_{50}x^{50}$ , for all  $x \in \mathbb{R}$ , then  $\frac{a_2}{a_0}$  is equal to :-  
 (1) 12.50      (2) 12.00      (3) 12.75      (4) 12.25

**Ans. (4)**

8. Let a function  $f : (0, \infty) \rightarrow (0, \infty)$  be defined by  $f(x) = \left| 1 - \frac{1}{x} \right|$ . Then  $f$  is :-  
 (1) Injective only  
 (2) Not injective but it is surjective  
 (3) Both injective as well as surjective  
 (4) Neither injective nor surjective

**Ans. (Bonus)**

9. Let  $S = \{1, 2, \dots, 20\}$ . A subset  $B$  of  $S$  is said to be "nice", if the sum of the elements of  $B$  is 203. Then the probability that a randomly chosen subset of  $S$  is "nice" is :-  
 (1)  $\frac{6}{2^{20}}$       (2)  $\frac{5}{2^{20}}$       (3)  $\frac{4}{2^{20}}$       (4)  $\frac{7}{2^{20}}$

**Ans. (2)**

10. Two lines  $\frac{x-3}{1} = \frac{y+1}{3} = \frac{z-6}{-1}$  and  $\frac{x+5}{7} = \frac{y-2}{-6} = \frac{z-3}{4}$  intersect at the point  $R$ . The reflection of  $R$  in the  $xy$ -plane has coordinates :-  
 (1)  $(2, 4, 7)$       (2)  $(-2, 4, 7)$   
 (3)  $(2, -4, -7)$       (4)  $(2, -4, 7)$

**Ans. (3)**

11. The number of functions  $f$  from  $\{1, 2, 3, \dots, 20\}$  onto  $\{1, 2, 3, \dots, 20\}$  such that  $f(k)$  is a multiple of 3, whenever  $k$  is a multiple of 4, is :-

- (1)  $(15)! \times 6!$                       (2)  $5^6 \times 15$   
 (3)  $5! \times 6!$                         (4)  $6^5 \times (15)!$

Ans. (1)

12. Contrapositive of the statement "If two numbers are not equal, then their squares are not equal." is :-

- (1) If the squares of two numbers are equal, then the numbers are equal.  
 (2) If the squares of two numbers are equal, then the numbers are not equal.  
 (3) If the squares of two numbers are not equal, then the numbers are equal.  
 (4) If the squares of two numbers are not equal, then the numbers are not equal.

Ans. (1)

13. The solution of the differential equation,

$$\frac{dy}{dx} = (x - y)^2, \text{ when } y(1) = 1, \text{ is :-}$$

(1)  $\log_e \left| \frac{2-y}{2-x} \right| = 2(y-1)$

(2)  $\log_e \left| \frac{2-x}{2-y} \right| = x-y$

(3)  $-\log_e \left| \frac{1+x-y}{1-x+y} \right| = x+y-2$

(4)  $-\log_e \left| \frac{1-x+y}{1+x-y} \right| = 2(x-1)$

Ans. (4)

14. Let  $A$  and  $B$  be two invertible matrices of order  $3 \times 3$ . If  $\det(ABA^T) = 8$  and  $\det(AB^{-1}) = 8$ , then  $\det(BA^{-1}B^T)$  is equal to :-

- (1) 16            (2)  $\frac{1}{16}$             (3)  $\frac{1}{4}$             (4) 1

Ans. (2)

15. If  $\int \frac{x+1}{\sqrt{2x-1}} dx = f(x)\sqrt{2x-1} + C$ , where  $C$  is a constant of integration, then  $f(x)$  is equal to :-

- (1)  $\frac{1}{3}(x+4)$                       (2)  $\frac{1}{3}(x+1)$   
 (3)  $\frac{2}{3}(x+2)$                       (4)  $\frac{2}{3}(x-4)$

Ans. (1)

16. A bag contains 30 white balls and 10 red balls. 16 balls are drawn one by one randomly from the bag with replacement. If  $X$  be the number of white balls drawn, the

$\left( \frac{\text{mean of } X}{\text{standard deviation of } X} \right)$  is equal to :-

- (1) 4            (2)  $\frac{4\sqrt{3}}{3}$             (3)  $4\sqrt{3}$             (4)  $3\sqrt{2}$

Ans. (3)

17. If in a parallelogram  $ABDC$ , the coordinates of  $A, B$  and  $C$  are respectively  $(1, 2), (3, 4)$  and  $(2, 5)$ , then the equation of the diagonal  $AD$  is:-

- (1)  $5x + 3y - 11 = 0$             (2)  $3x - 5y + 7 = 0$   
 (3)  $3x + 5y - 13 = 0$             (4)  $5x - 3y + 1 = 0$

Ans. (4)

18. If a hyperbola has length of its conjugate axis equal to 5 and the distance between its foci is 13, then the eccentricity of the hyperbola is :-

- (1) 2            (2)  $\frac{13}{6}$             (3)  $\frac{13}{8}$             (4)  $\frac{13}{12}$

Ans. (4)

19. The area (in sq. units) in the first quadrant bounded by the parabola,  $y = x^2 + 1$ , the tangent to it at the point  $(2, 5)$  and the coordinate axes is :-

- (1)  $\frac{14}{3}$             (2)  $\frac{187}{24}$             (3)  $\frac{37}{24}$             (4)  $\frac{8}{3}$

Ans. (3)

20. Let  $\sqrt{3}\hat{i} + \hat{j}, \hat{i} + \sqrt{3}\hat{j}$  and

$\beta\hat{i} + (1-\beta)\hat{j}$  respectively be the position vectors of the points  $A, B$  and  $C$  with respect to the origin  $O$ . If the distance of  $C$  from the bisector of the acute angle between  $OA$  and  $OB$  is  $\frac{3}{\sqrt{2}}$ ,

then the sum of all possible values of  $\beta$  is :-

(1) 2            (2) 1            (3) 3            (4) 4

Ans. (2)

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JEE (Advanced)- Target 2019

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21. If 
$$\begin{vmatrix} a-b-c & 2a & 2a \\ 2b & b-c-a & 2b \\ 2c & 2c & c-a-b \end{vmatrix}$$
  
 $= (a + b + c) (x + a + b + c)^2$ ,  $x \neq 0$  and  $a + b + c \neq 0$ , then  $x$  is equal to :-  
 (1)  $-(a + b + c)$                       (2)  $2(a + b + c)$   
 (3)  $abc$                                       (4)  $-2(a + b + c)$

**Ans. (4)**

22. Let  $S_n = 1 + q + q^2 + \dots + q^n$  and  

$$T_n = 1 + \left(\frac{q+1}{2}\right) + \left(\frac{q+1}{2}\right)^2 + \dots + \left(\frac{q+1}{2}\right)^n$$
  
 where  $q$  is a real number and  $q \neq 1$ .  
 If  ${}^{101}C_1 + {}^{101}C_2 \cdot S_1 + \dots + {}^{101}C_{101} \cdot S_{100} = \alpha T_{100}$ ,  
 then  $\alpha$  is equal to :-  
 (1)  $2^{100}$                       (2)  $200$                       (3)  $2^{99}$                       (4)  $202$

**Ans. (1)**

23. A circle cuts a chord of length  $4a$  on the  $x$ -axis and passes through a point on the  $y$ -axis, distant  $2b$  from the origin. Then the locus of the centre of this circle, is :-  
 (1) A hyperbola                      (2) A parabola  
 (3) A straight line                      (4) An ellipse

**Ans. (2)**

24. If 19th term of a non-zero A.P. is zero, then its (49th term) : (29th term) is :-  
 (1)  $3 : 1$                       (2)  $4 : 1$                       (3)  $2 : 1$                       (4)  $1 : 3$

**Ans. (1)**

25. Let  $f(x) = \frac{x}{\sqrt{a^2 + x^2}} - \frac{d-x}{\sqrt{b^2 + (d-x)^2}}$ ,  $x \in \mathbb{R}$ ,  
 where  $a, b$  and  $d$  are non-zero real constants.  
 Then :-  
 (1)  $f$  is a decreasing function of  $x$   
 (2)  $f$  is neither increasing nor decreasing function of  $x$   
 (3)  $f'$  is not a continuous function of  $x$   
 (4)  $f$  is an increasing function of  $x$

**Ans. (4)**

26. Let  $z$  be a complex number such that  $|z| + z = 3 + i$  (where  $i = \sqrt{-1}$ ). Then  $|z|$  is equal to :-

- (1)  $\frac{5}{4}$                       (2)  $\frac{\sqrt{41}}{4}$                       (3)  $\frac{\sqrt{34}}{3}$                       (4)  $\frac{5}{3}$

**Ans. (4)**

27. All  $x$  satisfying the inequality  $(\cot^{-1} x)^2 - 7(\cot^{-1} x) + 10 > 0$ , lie in the interval:-  
 (1)  $(-\infty, \cot 5) \cup (\cot 4, \cot 2)$   
 (2)  $(\cot 5, \cot 4)$   
 (3)  $(\cot 2, \infty)$   
 (4)  $(-\infty, \cot 5) \cup (\cot 2, \infty)$

**Ans. (4)**

28. Given  $\frac{b+c}{11} = \frac{c+a}{12} = \frac{a+b}{13}$  for a  $\Delta ABC$  with usual notation. If  $\frac{\cos A}{\alpha} = \frac{\cos B}{\beta} = \frac{\cos C}{\gamma}$ , then the ordered triad  $(\alpha, \beta, \gamma)$  has a value :-  
 (1)  $(3, 4, 5)$                       (2)  $(19, 7, 25)$   
 (3)  $(7, 19, 25)$                       (4)  $(5, 12, 13)$

**Ans. (3)**

29. Let  $x, y$  be positive real numbers and  $m, n$  positive integers. The maximum value of the expression  $\frac{x^m y^n}{(1+x^{2m})(1+y^{2n})}$  is :-

- (1)  $\frac{1}{2}$                       (2)  $\frac{1}{4}$                       (3)  $\frac{m+n}{6mn}$                       (4)  $1$

**Ans. (2)**

30.  $\lim_{x \rightarrow 0} \frac{x \cot(4x)}{\sin^2 x \cot^2(2x)}$  is equal to :-  
 (1)  $2$                       (2)  $0$                       (3)  $4$                       (4)  $1$

**Ans. (4)**

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**JEE (Main)- Target 2019**

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